Interaction of cosmic rays with molecular clouds

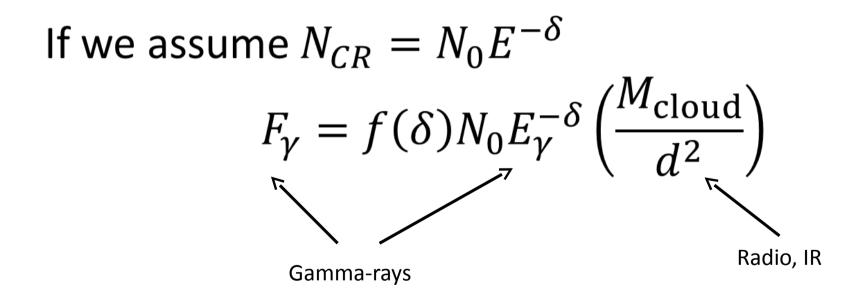
Chernyshov D.O Dogiel V.A., Cheng K.S., Ko C.M.

Why molecular clouds?

- They are dense (x1000 ISM)
 - All processes proportinal to density are increased!
- They are cold (10 100 K)
 - All thermal processes are low-energetic
 - All high-energy processes are due to external sources
- Space calorimeters

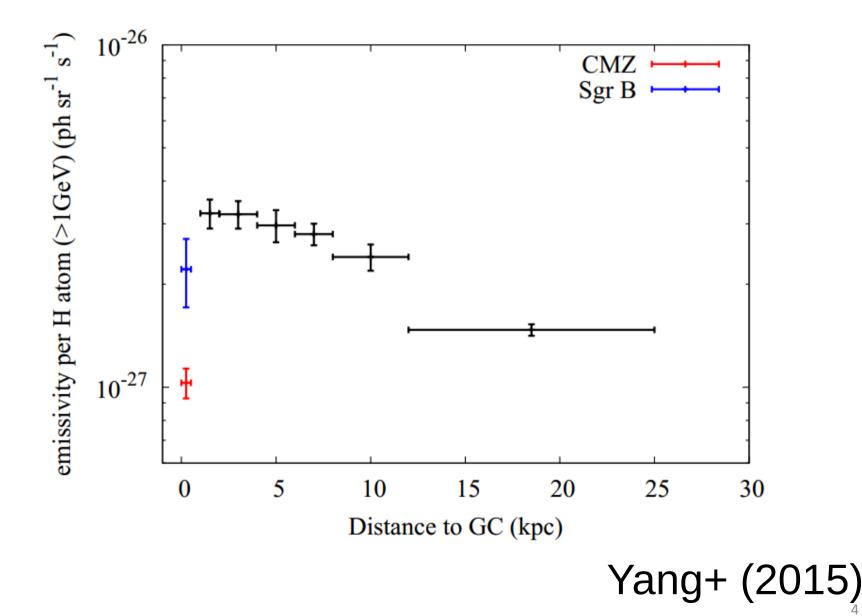
Molecular clouds as tracers of CRp

•
$$L_{\gamma} = n_{gas} N_{CR} (14E_{\gamma}) \sigma_{pp} c V_{cl} \propto M_{cl} N_{CR} (14E_{\gamma})$$

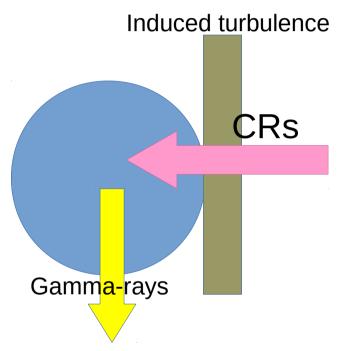


Black & Fazio 1973, Issa & Wolfendale 1981, Aharonian 1991, Casanova et al. 2010

CRs from diffuse molecular gas



Molecular clouds as CR "sinks"



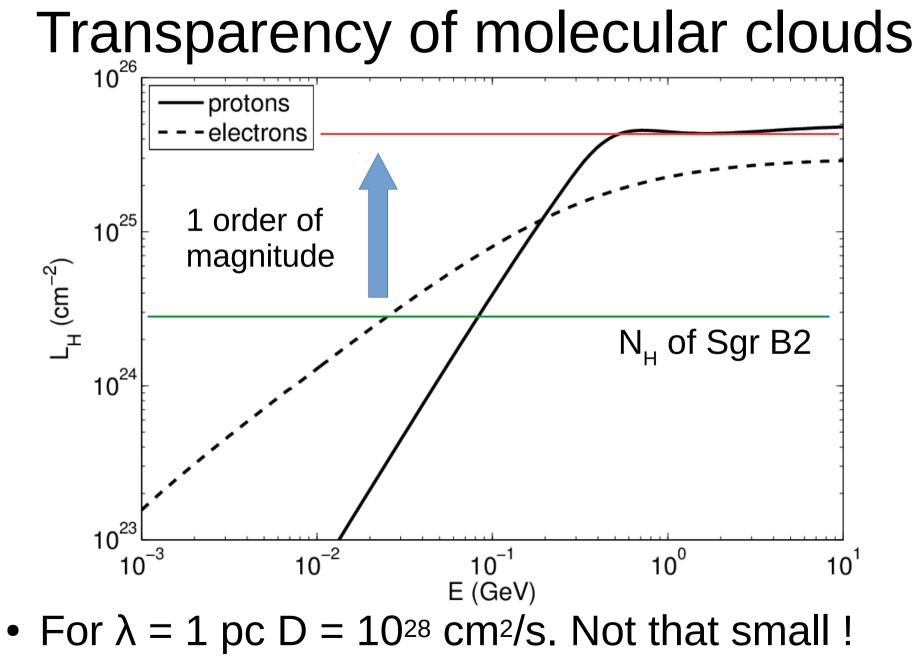
For Sgr B2 we know:

- Luminosity is 7x10³⁵ erg/s
- Size is 12 pc
- CR density is 1 eV/cm³
- Ionization rate 10⁻¹⁵ s⁻¹
- Ambient density is 100 cm⁻³
- B = 10 uG

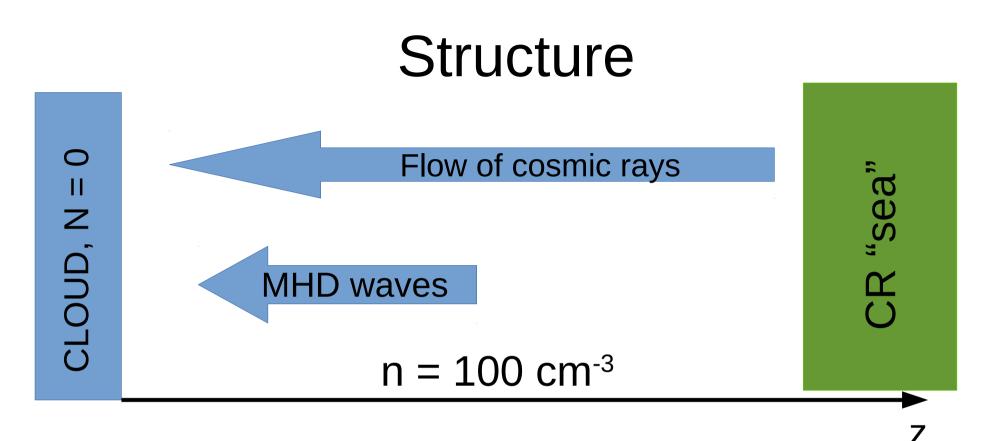
•
$$V_A = 10^8 \text{ cm/s}$$

For gamma-rays $v_s = \frac{L}{\epsilon S} = 2.8 \times 10^7 \, cm/s$

Given 30% initial proton energy goes into gamma-rays streaming velocity of protons is close to v_a (c.f. Morlino&Gabici 2015)



CRBTSM - 2, San Vito di Cadore, 2016



- For simplicity assume that only self-generated turbulence exists
- Let's assume thick-target model i.e. N(0) = 0
- It should be correct if cloud is dense and $D_{cloud} >> D_{inter}$

Equations for wave+particles

$$\frac{\partial N}{\partial t} - \frac{\partial}{\partial z} \left(D(z, E) \frac{\partial N}{\partial z} - v_A N \right) + \left[\frac{\partial}{\partial E} \left(\frac{dE}{dt} N \right) \right] = 0$$
$$\frac{\partial W}{\partial t} + v_A \frac{\partial W}{\partial z} + \frac{\partial}{\partial k} \left(\frac{k W(k)}{T_{nl}} \right) = 2(\Gamma_{CR} - \nu_{in})W,$$

$$\Gamma_{cr} \simeq \frac{\gamma - 1}{\gamma} \frac{\pi}{4} \Omega_{Hi} \frac{N(>p_{res})}{n_i} \left(\frac{u_0}{v_A} - 1\right)$$

Important value – advection vs diffusion regime

$$\zeta = \int_{0}^{z} \frac{v_A dx}{D(x)}$$

CRBTSM - 2, San Vito di Cadore, 2016

Analytic approximation

No losses or damping. Non-relativistic regime

$$\frac{\partial}{\partial z} \left(\frac{\partial \zeta}{\partial \bar{k}} - \frac{3}{2} \frac{\zeta}{\bar{k}} \right) = B \left(\frac{\exp(-\zeta)}{1 - \exp(-\zeta)} \right) \int_{k_{min}}^{k} y^{-0.4} \left[1 - \exp(-\zeta(y)) \right] dy$$

In the "convection" region $\zeta > 1$ that gives $\frac{\zeta}{\bar{k}^{3/2}} = const$
Fully-trapped particles (c.f. Morlino&Gabici 2015)
Should exist far away from boundaries i.e.

$$\zeta = \int_{0}^{z} \frac{v_{A} dx}{D(x)} = \int_{0}^{z_{0}} \frac{v_{A} dx}{D(x)} + \int_{z_{0}}^{z} \frac{v_{A} dx}{D(x)} = const$$

CRBTSM - 2, San Vito di Cadore, 2016

Analytic approximation

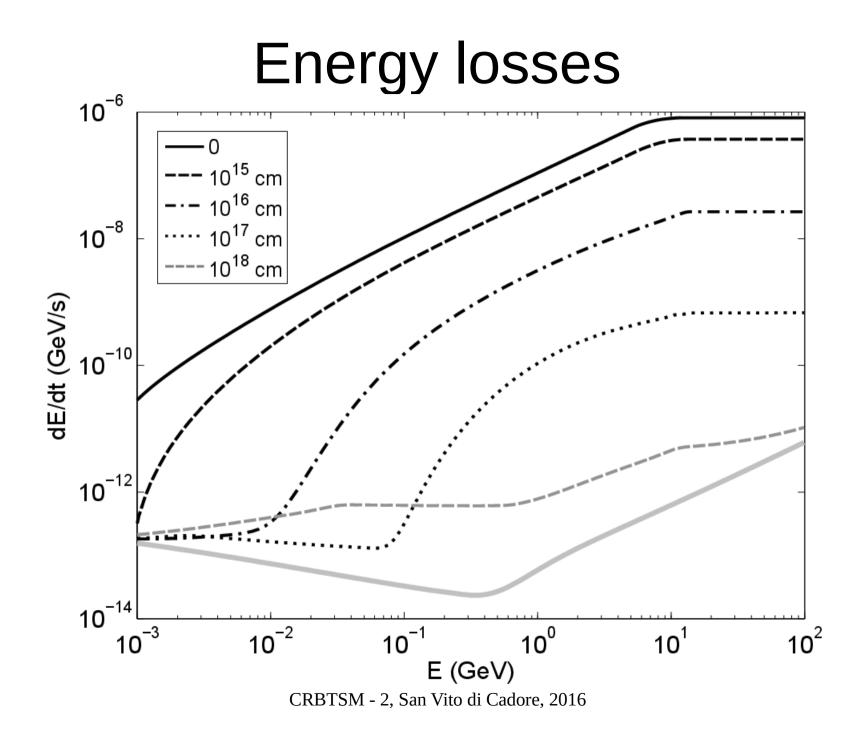
In the diffusion regime where $\zeta << 1$ variables can be split and $\zeta(k,z) = \zeta(k)z$

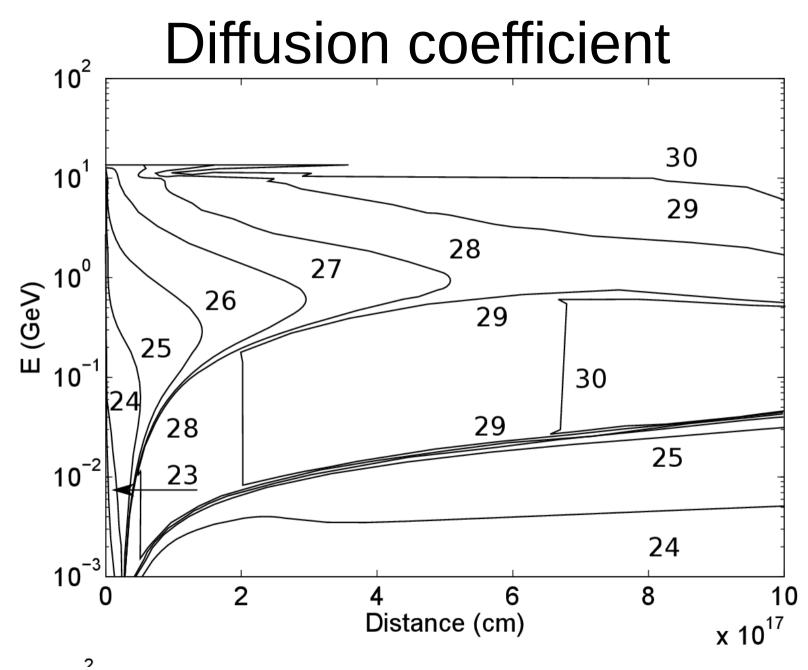
It causes D(k,z) = D(k) and N(p,z) = N(p)z

However in this case average streaming velocity is

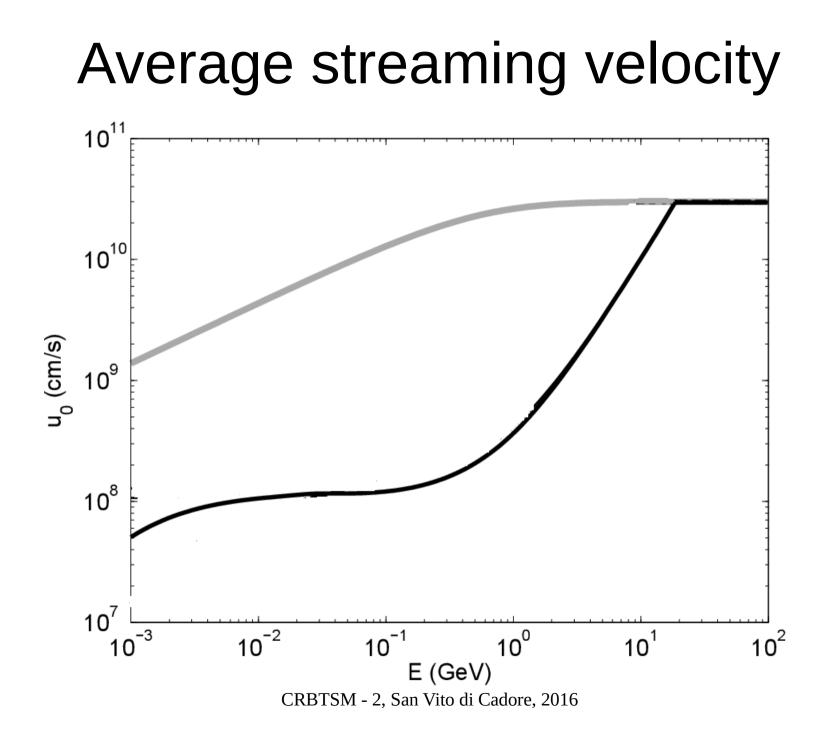
$$v_s = \frac{S}{N} \propto z^{-1}$$

It may (and will!) exceed proper particle velocity Different transport equation required!

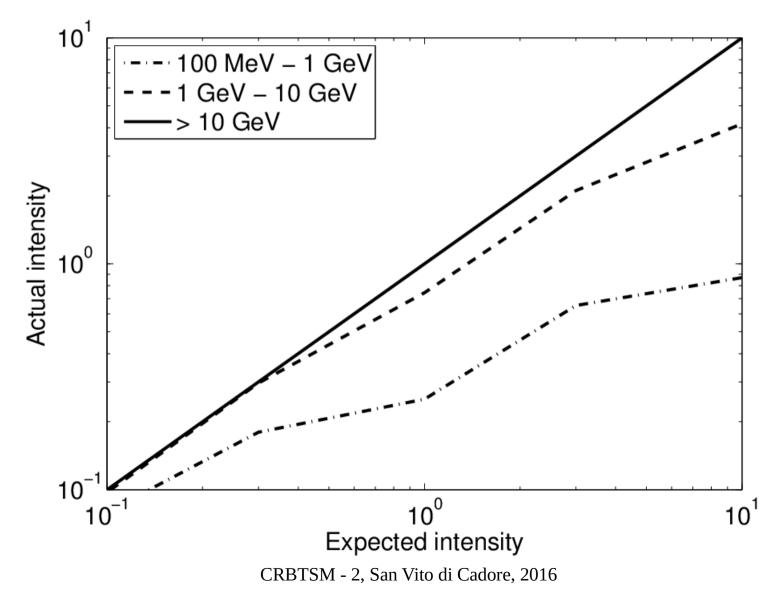




CRBTSM - 2, San Vito di Cadore, 2016



Suppression of gamma-ray emission



Conclusions

- Self-generated turbulence is important for particle-cloud interactions
- Super-luminal velocities are expected in the case of diffusion equation
- Self-generated turbulence mainly affects subrelativistic particles yet may also suppress gamma-ray emission

Additional slide 1

$$\frac{\partial f}{\partial t} + \operatorname{div} S + \left(\frac{\partial}{\partial E}\frac{dE}{dt}f\right) = 0$$
$$S = \min\left\{-D\nabla f, v \cdot f\right\},$$

$$D(E) = \frac{vH^2}{12\pi k_{res}^2 W(k_{res})}$$

$$\frac{dE}{dt} = \frac{\gamma - 1}{\gamma} \frac{\pi}{4} \frac{\Omega_{Hi}}{n_i} \int_{k_{res}}^{k_{max}} W\left(\frac{u_0}{v_a} - 1\right) dk$$

CRBTSM - 2, San Vito di Cadore, 2016